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In[1]:= TextCell["Gell-Mann matrices"]
λ1 = {{0, 1, 0}, {1, 0, 0}, {0, 0, 0}}
λ2 = {{0, -I, 0}, {I, 0, 0}, {0, 0, 0}}
λ3 = {{1, 0, 0}, {0, -1, 0}, {0, 0, 0}}
λ4 = {{0, 0, 1}, {0, 0, 0}, {1, 0, 0}}
λ5 = {{0, 0, -I}, {0, 0, 0}, {I, 0, 0}}
λ6 = {{0, 0, 0}, {0, 0, 1}, {0, 1, 0}}
λ7 = {{0, 0, 0}, {0, 0, -I}, {0, I, 0}}
λ8 = (1 / Sqrt[3]) * {{1, 0, 0}, {0, 1, 0}, {0, 0, -2}}
b11 = ConjugateTranspose[λ1].λ1
b21 = ConjugateTranspose[λ1].λ2
b31 = ConjugateTranspose[λ1].λ3
b41 = ConjugateTranspose[λ1].λ4
b51 = ConjugateTranspose[λ1].λ5
b61 = ConjugateTranspose[λ1].λ6
b71 = ConjugateTranspose[λ1].λ7
b81 = ConjugateTranspose[λ1].λ8
b12 = ConjugateTranspose[λ2].λ1
b22 = ConjugateTranspose[λ2].λ2
b32 = ConjugateTranspose[λ2].λ3
b42 = ConjugateTranspose[λ2].λ4
b52 = ConjugateTranspose[λ2].λ5
b62 = ConjugateTranspose[λ2].λ6
b72 = ConjugateTranspose[λ2].λ7
b82 = ConjugateTranspose[λ2].λ8
b13 = ConjugateTranspose[λ3].λ1
b23 = ConjugateTranspose[λ3].λ2
b33 = ConjugateTranspose[λ3].λ3
b43 = ConjugateTranspose[λ3].λ4
b53 = ConjugateTranspose[λ3].λ5
b63 = ConjugateTranspose[λ3].λ6
b73 = ConjugateTranspose[λ3].λ7
b83 = ConjugateTranspose[λ3].λ8
b14 = ConjugateTranspose[λ4].λ1
b24 = ConjugateTranspose[λ4].λ2
b34 = ConjugateTranspose[λ4].λ3
b44 = ConjugateTranspose[λ4].λ4
b54 = ConjugateTranspose[λ4].λ5
b64 = ConjugateTranspose[λ4].λ6
b74 = ConjugateTranspose[λ4].λ7
b84 = ConjugateTranspose[λ4].λ8
b15 = ConjugateTranspose[λ5].λ1
b25 = ConjugateTranspose[λ5].λ2
b35 = ConjugateTranspose[λ5].λ3
b45 = ConjugateTranspose[λ5].λ4
b55 = ConjugateTranspose[λ5].λ5
b65 = ConjugateTranspose[λ5].λ6
b75 = ConjugateTranspose[λ5].λ7
b85 = ConjugateTranspose[λ5].λ8
b16 = ConjugateTranspose[λ6].λ1
b26 = ConjugateTranspose[λ6].λ2

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b36 = ConjugateTranspose[λ6].λ3
b46 = ConjugateTranspose[λ6].λ4
b56 = ConjugateTranspose[λ6].λ5
b66 = ConjugateTranspose[λ6].λ6
b76 = ConjugateTranspose[λ6].λ7
b86 = ConjugateTranspose[λ6].λ8
b17 = ConjugateTranspose[λ7].λ1
b27 = ConjugateTranspose[λ7].λ2
b37 = ConjugateTranspose[λ7].λ3
b47 = ConjugateTranspose[λ7].λ4
b57 = ConjugateTranspose[λ7].λ5
b67 = ConjugateTranspose[λ7].λ6
b77 = ConjugateTranspose[λ7].λ7
b87 = ConjugateTranspose[λ7].λ8
b18 = ConjugateTranspose[λ8].λ1
b28 = ConjugateTranspose[λ8].λ2
b38 = ConjugateTranspose[λ8].λ3
b48 = ConjugateTranspose[λ8].λ4
b58 = ConjugateTranspose[λ8].λ5
b68 = ConjugateTranspose[λ8].λ6
b78 = ConjugateTranspose[λ8].λ7
b88 = ConjugateTranspose[λ8].λ8
M = {b11, b21, b31, b41, b51, b61, b71, b81, b12, b22, b32, b42, b52, b62, b72,
      b82, b13, b23, b33, b43, b53, b63, b73, b83, b14, b24, b34, b44, b54, b64, b74,
      b84, b15, b25, b35, b45, b55, b65, b75, b85, b16, b26, b36, b46, b56, b66, b76, b86,
      b17, b27, b37, b47, b57, b67, b77, b87, b18, b28, b38, b48, b58, b68, b78, b88}
V = Map[Flatten, M]
linearIndependenceQ = Not[RowReduce[V][[-1]] == Table[0, {3}]]
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Out[1]= Gell-Mann matrices

Out[2]= {{0, 1, 0}, {1, 0, 0}, {0, 0, 0}}

Out[3]= {{0, -i, 0}, {i, 0, 0}, {0, 0, 0}}

Out[4]= {{1, 0, 0}, {0, -1, 0}, {0, 0, 0}}

Out[5]= {{0, 0, 1}, {0, 0, 0}, {1, 0, 0}}

Out[6]= {{0, 0, -i}, {0, 0, 0}, {i, 0, 0}}

Out[7]= {{0, 0, 0}, {0, 0, 1}, {0, 1, 0}}

Out[8]= {{0, 0, 0}, {0, 0, -i}, {0, i, 0}}

Out[9]=  $\left\{ \left\{ \frac{1}{\sqrt{3}}, 0, 0 \right\}, \left\{ 0, \frac{1}{\sqrt{3}}, 0 \right\}, \left\{ 0, 0, -\frac{2}{\sqrt{3}} \right\} \right\}$

Out[10]= {{1, 0, 0}, {0, 1, 0}, {0, 0, 0}}

Out[11]= {{i, 0, 0}, {0, -i, 0}, {0, 0, 0}}

Out[12]= {{0, -1, 0}, {1, 0, 0}, {0, 0, 0}}

Out[13]= {{0, 0, 0}, {0, 0, 1}, {0, 0, 0}}

Out[14]= {{0, 0, 0}, {0, 0, -i}, {0, 0, 0}}

Out[15]= {{0, 0, 1}, {0, 0, 0}, {0, 0, 0}}

Out[16]= {{0, 0, -i}, {0, 0, 0}, {0, 0, 0}}

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Out[17]=  $\left\{\left\{0, \frac{1}{\sqrt{3}}, 0\right\}, \left\{\frac{1}{\sqrt{3}}, 0, 0\right\}, \{0, 0, 0\}\right\}$ 
Out[18]=  $\{\{-\text{i}, 0, 0\}, \{0, \text{i}, 0\}, \{0, 0, 0\}\}$ 
Out[19]=  $\{\{1, 0, 0\}, \{0, 1, 0\}, \{0, 0, 0\}\}$ 
Out[20]=  $\{\{0, \text{i}, 0\}, \{\text{i}, 0, 0\}, \{0, 0, 0\}\}$ 
Out[21]=  $\{\{0, 0, 0\}, \{0, 0, \text{i}\}, \{0, 0, 0\}\}$ 
Out[22]=  $\{\{0, 0, 0\}, \{0, 0, 1\}, \{0, 0, 0\}\}$ 
Out[23]=  $\{\{0, 0, -\text{i}\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[24]=  $\{\{0, 0, -1\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[25]=  $\left\{\left\{0, -\frac{\text{i}}{\sqrt{3}}, 0\right\}, \left\{\frac{\text{i}}{\sqrt{3}}, 0, 0\right\}, \{0, 0, 0\}\right\}$ 
Out[26]=  $\{\{0, 1, 0\}, \{-1, 0, 0\}, \{0, 0, 0\}\}$ 
Out[27]=  $\{\{0, -\text{i}, 0\}, \{-\text{i}, 0, 0\}, \{0, 0, 0\}\}$ 
Out[28]=  $\{\{1, 0, 0\}, \{0, 1, 0\}, \{0, 0, 0\}\}$ 
Out[29]=  $\{\{0, 0, 1\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[30]=  $\{\{0, 0, -\text{i}\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[31]=  $\{\{0, 0, 0\}, \{0, 0, -1\}, \{0, 0, 0\}\}$ 
Out[32]=  $\{\{0, 0, 0\}, \{0, 0, \text{i}\}, \{0, 0, 0\}\}$ 
Out[33]=  $\left\{\left\{\frac{1}{\sqrt{3}}, 0, 0\right\}, \left\{0, -\frac{1}{\sqrt{3}}, 0\right\}, \{0, 0, 0\}\right\}$ 
Out[34]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{0, 1, 0\}\}$ 
Out[35]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{0, -\text{i}, 0\}\}$ 
Out[36]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{1, 0, 0\}\}$ 
Out[37]=  $\{\{1, 0, 0\}, \{0, 0, 0\}, \{0, 0, 1\}\}$ 
Out[38]=  $\{\{\text{i}, 0, 0\}, \{0, 0, 0\}, \{0, 0, -\text{i}\}\}$ 
Out[39]=  $\{\{0, 1, 0\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[40]=  $\{\{0, \text{i}, 0\}, \{0, 0, 0\}, \{0, 0, 0\}\}$ 
Out[41]=  $\left\{\left\{0, 0, -\frac{2}{\sqrt{3}}\right\}, \{0, 0, 0\}, \left\{\frac{1}{\sqrt{3}}, 0, 0\right\}\right\}$ 
Out[42]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{0, \text{i}, 0\}\}$ 
Out[43]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{0, 1, 0\}\}$ 
Out[44]=  $\{\{0, 0, 0\}, \{0, 0, 0\}, \{\text{i}, 0, 0\}\}$ 
Out[45]=  $\{\{-\text{i}, 0, 0\}, \{0, 0, 0\}, \{0, 0, \text{i}\}\}$ 

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Out[46]= {{1, 0, 0}, {0, 0, 0}, {0, 0, 1}}
Out[47]= {{0, -I, 0}, {0, 0, 0}, {0, 0, 0}}
Out[48]= {{0, 1, 0}, {0, 0, 0}, {0, 0, 0}}
Out[49]= {{0, 0, 2 I / Sqrt[3]}, {0, 0, 0}, {I / Sqrt[3], 0, 0}}
Out[50]= {{0, 0, 0}, {0, 0, 0}, {1, 0, 0}}
Out[51]= {{0, 0, 0}, {0, 0, 0}, {I, 0, 0}}
Out[52]= {{0, 0, 0}, {0, 0, 0}, {0, -1, 0}}
Out[53]= {{0, 0, 0}, {1, 0, 0}, {0, 0, 0}}
Out[54]= {{0, 0, 0}, {I, 0, 0}, {0, 0, 0}}
Out[55]= {{0, 0, 0}, {0, 1, 0}, {0, 0, 1}}
Out[56]= {{0, 0, 0}, {0, I, 0}, {0, 0, -I}}
Out[57]= {{0, 0, 0}, {0, 0, -2 / Sqrt[3]}, {0, 1 / Sqrt[3], 0}}
Out[58]= {{0, 0, 0}, {0, 0, 0}, {I, 0, 0}}
Out[59]= {{0, 0, 0}, {0, 0, 0}, {-1, 0, 0}}
Out[60]= {{0, 0, 0}, {0, 0, 0}, {0, -I, 0}}
Out[61]= {{0, 0, 0}, {-I, 0, 0}, {0, 0, 0}}
Out[62]= {{0, 0, 0}, {1, 0, 0}, {0, 0, 0}}
Out[63]= {{0, 0, 0}, {0, -I, 0}, {0, 0, I}}
Out[64]= {{0, 0, 0}, {0, 1, 0}, {0, 0, 1}}
Out[65]= {{0, 0, 0}, {0, 0, 2 I / Sqrt[3]}, {0, I / Sqrt[3], 0}}
Out[66]= {{0, 1 / Sqrt[3], 0}, {1 / Sqrt[3], 0, 0}, {0, 0, 0}}
Out[67]= {{0, -I / Sqrt[3], 0}, {I / Sqrt[3], 0, 0}, {0, 0, 0}}
Out[68]= {{1 / Sqrt[3], 0, 0}, {0, -1 / Sqrt[3], 0}, {0, 0, 0}}
Out[69]= {{0, 0, 1 / Sqrt[3]}, {0, 0, 0}, {-2 / Sqrt[3], 0, 0}}
Out[70]= {{0, 0, -I / Sqrt[3]}, {0, 0, 0}, {-2 I / Sqrt[3], 0, 0}}

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$$\text{Out}[71]= \left\{ \{0, 0, 0\}, \left\{0, 0, \frac{1}{\sqrt{3}}\right\}, \left\{0, -\frac{2}{\sqrt{3}}, 0\right\} \right\}$$

$$\text{Out}[72]= \left\{ \{0, 0, 0\}, \left\{0, 0, -\frac{\frac{1}{2} i}{\sqrt{3}}\right\}, \left\{0, -\frac{2 \frac{1}{2} i}{\sqrt{3}}, 0\right\} \right\}$$

$$\text{Out}[73]= \left\{ \left\{\frac{1}{3}, 0, 0\right\}, \left\{0, \frac{1}{3}, 0\right\}, \left\{0, 0, \frac{4}{3}\right\} \right\}$$

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Out[74]= \{\{\{1, 0, 0\}, {0, 1, 0\}, {0, 0, 0\}\}, {\{i, 0, 0\}, {0, -i, 0\}, {0, 0, 0\}\},
\{\{0, -1, 0\}, {1, 0, 0\}, {0, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, 1\}, {0, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, -i\}, {0, 0, 0\}\}, {\{0, 0, 1\}, {0, 0, 0\}, {0, 0, 0\}\},
\{\{0, 0, -i\}, {0, 0, 0\}, {0, 0, 0\}\}, \{\{0, \frac{1}{\sqrt{3}}, 0\}, \{\frac{1}{\sqrt{3}}, 0, 0\}, {0, 0, 0\}\},
\{\{-i, 0, 0\}, {0, i, 0\}, {0, 0, 0\}\}, {\{1, 0, 0\}, {0, 1, 0\}, {0, 0, 0\}\},
\{\{0, i, 0\}, {i, 0, 0\}, {0, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, i\}, {0, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, 1\}, {0, 0, 0\}\}, {\{0, 0, -i\}, {0, 0, 0\}, {0, 0, 0\}\},
\{\{0, 0, -1\}, {0, 0, 0\}, {0, 0, 0\}\}, \{\{0, -\frac{i}{\sqrt{3}}, 0\}, \{\frac{i}{\sqrt{3}}, 0, 0\}, {0, 0, 0\}\},
\{\{0, 1, 0\}, {-1, 0, 0\}, {0, 0, 0\}\}, {\{0, -i, 0\}, {-i, 0, 0\}, {0, 0, 0\}\},
\{\{1, 0, 0\}, {0, 1, 0\}, {0, 0, 0\}\}, {\{0, 0, 1\}, {0, 0, 0\}, {0, 0, 0\}\},
\{\{0, 0, -i\}, {0, 0, 0\}, {0, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, -1\}, {0, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, i\}, {0, 0, 0\}\}, \{\{\frac{1}{\sqrt{3}}, 0, 0\}, \{0, -\frac{1}{\sqrt{3}}, 0\}, {0, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {0, 1, 0\}\}, {\{0, 0, 0\}, {0, 0, 0\}, {0, -i, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {1, 0, 0\}\}, {\{1, 0, 0\}, {0, 0, 0\}, {0, 0, 1\}\},
\{\{i, 0, 0\}, {0, 0, 0\}, {0, 0, -i\}\}, {\{0, 1, 0\}, {0, 0, 0\}, {0, 0, 0\}\},
\{\{0, i, 0\}, {0, 0, 0\}, {0, 0, 0\}\}, {\{0, 0, -\frac{2}{\sqrt{3}}\}, {0, 0, 0\}, \{\frac{1}{\sqrt{3}}, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {0, i, 0\}\}, {\{0, 0, 0\}, {0, 0, 0\}, {0, 1, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {i, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, 0\}, {0, 0, i\}\},
\{\{1, 0, 0\}, {0, 0, 0\}, {0, 0, 1\}\}, {\{0, 0, -i\}, {0, 0, 0\}, {0, 0, 0\}\},
\{\{0, 1, 0\}, {0, 0, 0\}, {0, 0, 0\}\}, \{\{0, 0, \frac{2i}{\sqrt{3}}\}, {0, 0, 0\}, \{\frac{i}{\sqrt{3}}, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {1, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, 0\}, {i, 0, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {0, -1, 0\}\}, {\{0, 0, 0\}, {1, 0, 0\}, {0, 0, 0\}\},
\{\{0, 0, 0\}, {i, 0, 0\}, {0, 0, 0\}\}, {\{0, 0, 0\}, {0, 1, 0\}, {0, 0, 1\}\},
\{\{0, 0, 0\}, {0, i, 0\}, {0, 0, -i\}\}, {\{0, 0, 0\}, {0, 0, -\frac{2}{\sqrt{3}}\}, {0, 0, \frac{1}{\sqrt{3}}, 0\}\},
\{\{0, 0, 0\}, {0, 0, 0\}, {i, 0, 0\}\}, {\{0, 0, 0\}, {0, 0, 0\}, {0, -i, 0\}\},
\{\{0, 0, 0\}, {0, 1, 0\}, {0, 0, 1\}\}, {\{0, 0, 0\}, {0, 0, \frac{2i}{\sqrt{3}}\}, {0, 0, \frac{i}{\sqrt{3}}, 0\}\},
\{\{0, 0, \frac{1}{\sqrt{3}}, 0\}, \{\frac{1}{\sqrt{3}}, 0, 0\}, {0, 0, 0\}\}, \{\{0, -\frac{i}{\sqrt{3}}, 0\}, \{\frac{i}{\sqrt{3}}, 0, 0\}, {0, 0, 0\}\},
\{\{\frac{1}{\sqrt{3}}, 0, 0\}, \{0, -\frac{1}{\sqrt{3}}, 0\}, {0, 0, 0\}\}, \{\{0, 0, \frac{1}{\sqrt{3}}\}, {0, 0, 0\}, \{-\frac{2}{\sqrt{3}}, 0, 0\}\},
\{\{0, 0, -\frac{i}{\sqrt{3}}\}, {0, 0, 0\}, \{-\frac{2i}{\sqrt{3}}, 0, 0\}\}, \{\{0, 0, 0\}, \{0, 0, \frac{1}{\sqrt{3}}\}, {0, -\frac{2}{\sqrt{3}}, 0\}\},
\{\{0, 0, 0\}, \{0, 0, -\frac{i}{\sqrt{3}}\}, \{0, -\frac{2i}{\sqrt{3}}, 0\}\}, \{\{\frac{1}{3}, 0, 0\}, \{0, \frac{1}{3}, 0\}, \{0, 0, \frac{4}{3}\}\}\}

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